



# Fixed-mobile substitution

A simultaneous equation model  
with qualitative and limited  
dependent variables

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# Background



- ❑ Rapidly increasing mobile penetration
- ❑ Regulatory interest in understanding the relationship between fixed and mobile services:
  - ❑ If complements: does not impact on fixed regulation
  - ❑ If substitutes: fixed regulation could be relaxed as the mobile sector is often largely competitive
- ❑ Naive interpretation of survey data suggest that fixed and mobile telephony are complements

# Forms of substitution

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- ❑ Access level substitution:  
more mobile phones → fewer fixed lines
- ❑ Call level substitution:  
higher mobile usage → lower fixed usage
- ❑ The two forms of substitution are linked as  
access decision is based on expected usage

# Empirical analysis



- ❑ Time series analysis of macro data suggest access level substitution (Pita Barros and Cadima 2000, DotEcon 2001), but data tend to be poor
- ❑ Analysis presented here is based on survey data
  - ❑ Repeated cross section (3 waves: 1999, 2000, 2001)
  - ❑ Telephone survey
  - ❑ >2000 observations per wave

# Controlling for tastes



- ❑ Statistics based on **observed fixed usage** might be misleading if there is **self selection** according to taste for telephony
- ❑ Need to establish fixed usage (expenditure) for the whole sample for **both** with and without mobile ownership, and then calculate statistics
- ❑ Fixed expenditure should be compared between the two scenarios across whole sample
- ❑ Endogenous switching models (Lee 1978, Maddala 1983, Trost 1981)

# Endogenous switching model



- ❑ Individual buys a phone if expected reduction in fixed bill is sufficiently large
- ❑ We cannot observe the fixed bill a mobile user would have if he/she did not have a mobile phone
- ❑ Comparing observed fixed bills of mobile and non-mobile users is misleading as it does not take account of self-selection
- ❑ Consistent estimation of fixed bill requires the introduction of a selectivity term

# Theoretical background I



Individual  $i$  buys a mobile phone if:

$$Y_{ni} - Y_{mi} > h_i \quad (Y_m: \text{fixed bill with mobile, } Y_n: \text{fixed bill without mobile})$$

$$h_i = aX_i + e_i \quad (X: \text{individual characteristics})$$

Therefore for those who buy a mobile phone:

$$(Y_{ni} - Y_{mi}) - aX_i - e_i > 0$$

Which can be rewritten as a probit equation:

$$I_i^* = I_0 + I_1(Y_{ni} - Y_{mi}) + I_2X_i - e_i$$

# Theoretical background II



Fixed bill can be estimated as:

$$Y_{mi} = \mathbf{d}_{m0} + \mathbf{d}_{m1} X_{mi} + \mathbf{e}_{mi}$$

$$Y_{nj} = \mathbf{d}_{n0} + \mathbf{d}_{n1} X_{nj} + \mathbf{e}_{nj}$$

However, we can only observe fixed bill for special cases:

$Y_{mi}$  when  $I_i = 1$  and

$Y_{ni}$  when  $I_i = 0$ .

# Theoretical background III



Consistent estimation of the fixed bill equations requires the introduction of a selectivity term:

$$Y_{mi} = \mathbf{d}_{m0} + \mathbf{d}_{m1} X_{mi} + \mathbf{s}_{me} \frac{f(\Psi_i^*)}{1 - \Phi(\Psi_i^*)} + V_{mi} \quad \text{for } I_i = 1$$

$$Y_{ni} = \mathbf{d}_{n0} + \mathbf{d}_{n1} X_{ni} - \mathbf{s}_{ne} \frac{f(\Psi_i^*)}{\Phi(\Psi_i^*)} + V_{ni} \quad \text{for } I_i = 0$$

Where  $\Psi_i^*$  is the consistent estimate of the probability of having a mobile

# Estimation



1. Reduced form probit → calculate predicted probabilities
2. Fixed spending equations → calculate predicted spending for both scenarios
3. Structural probit

We use the following variables:

- Internet and fax usage
- Homeworker
- Gender, age, income, social class and household size dummies

# Results I



## Reduced form probit (3<sup>rd</sup> survey)

Variable	Coefficient	z-value
WWW	0.59	5.47
FAX	0.11	0.71
GENDER	0.26	2.75
HOMEW	-0.00	-0.02
Constant	0.97	1.94
Wald Chi2 (df=29)	213.68	
Observations	1048	

*Z-values are calculated using robust standard errors. Jointly significant social class, age, household size and income dummies are included*

# Results II



**Fixed telephony spending (selectivity adjusted for mobile phone owners, 3<sup>rd</sup> survey)**

<b>Variable</b>	<b>Coefficient</b>	<b>z-value</b>
<b>WWW</b>	7.36	1.54
<b>FAX</b>	23.53	5.65
<b>HOMEW</b>	13.81	3.14
<b>Constant</b>	-6.89	-0.17
<b>Selectivity parameter</b>	51.75	1.87
<b>Wald Chi2 (df=22)</b>	265.00	
<b>Observations</b>	751	

*Z-values are calculated using robust standard errors. Jointly significant social class, age, and household dummies are included*

# Results III



**Fixed telephony spending (selectivity adjusted for non-mobile users, 3<sup>rd</sup> survey)**

<b>Variable</b>	<b>Coefficient</b>	<b>z-value</b>
<b>WWW</b>	10.80	1.81
<b>HOMEW</b>	12.90	1.50
<b>Constant</b>	67.41	5.43
<b>Selectivity parameter</b>	33.23	1.64
<b>Wald Chi2 (df=8)</b>	68.87	
<b>Observations</b>	297	

*Z-values are calculated using robust standard errors. Jointly significant household size dummies are included*

# Results IV



Structural probit estimates (3<sup>rd</sup> survey)

Variable	Coefficient (probit)	Coefficient (dprobit)	z-value
<b>Yn-Ym</b>	0.01	0.003	1.70
<b>WWW</b>	0.53	0.16	4.95
<b>FAX</b>	0.40	0.11	1.86
<b>GENDER</b>	0.26	0.08	2.76
<b>HOMEW</b>	-0.01	0.00	0.04
<b>Constant</b>	-0.05		-0.09
<b>Wald Chi2 (df=20)</b>	210.43		
<b>Observations</b>	1048		

*Z-values are calculated using robust standard errors. Jointly significant age and income dummies are included.*

# Conclusions



- ❑ Strong evidence for call level substitution between fixed and mobile telephony as people decrease their fixed line usage as a result in mobile ownership
- ❑ Indirect evidence for access level substitution as the fall in fixed line expenditure creates an incentive to buy mobile phones